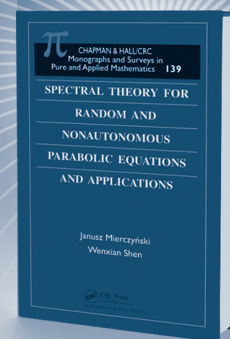


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# Spectral Theory for Random and Nonautonomous Parabolic Equations and Applications

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- Explores applications of the principal spectral theory to the uniform persistence of competitive Kolmogorov systems of nonautonomous and random parabolic equations

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